

CSE-5368 Neural Networks

Spring 2023

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$$F(\mathbf{x}) = F(\mathbf{x}^*) + \nabla F(\mathbf{x})^T \Big|_{\mathbf{x}=\mathbf{x}^*} (\mathbf{x} - \mathbf{x}^*) \\ + \frac{1}{2} (\mathbf{x} - \mathbf{x}^*)^T \nabla^2 F(\mathbf{x}) \Big|_{\mathbf{x}=\mathbf{x}^*} (\mathbf{x} - \mathbf{x}^*) + \dots$$

$$\frac{\mathbf{p}^T \nabla F(\mathbf{x})}{\|\mathbf{p}\|} \quad \frac{\mathbf{p}^T \nabla^2 F(\mathbf{x}) \mathbf{p}}{\|\mathbf{p}\|^2} \quad \alpha_k = - \frac{\mathbf{g}_k^T \mathbf{p}_k}{\mathbf{p}_k^T \mathbf{A} \mathbf{p}_k}$$

$$\mathbf{x}_{k+1} = \mathbf{x}_k - \alpha_k \mathbf{g}_k \quad \mathbf{x}_{k+1} = \mathbf{x}_k + \alpha_k \mathbf{p}_k \quad \mathbf{x}_{k+1} = \mathbf{x}_k - \mathbf{A}_k^{-1} \mathbf{g}_k$$

$$S(y_i) = \frac{e^{y_i}}{\sum_j e^{y_j}}$$

$$H(p, q) = - \sum_x p(x) \log(q(x))$$

$$L_i = - \log \left(\frac{e^{y_i}}{\sum_j e^{y_j}} \right)$$

$$L_i = \sum_{j \neq i} \max(0, y_j - y_i + \Delta)$$

$$\frac{\partial \tanh(x)}{\partial x} = 1 - (\tanh(x))^2$$

$$\frac{\partial \sigma(x)}{\partial x} = (\sigma(x))(1 - \sigma(x))$$

$$N = Wx + b$$

$$\frac{\partial \text{loss}}{\partial W} = \frac{\partial \text{loss}}{\partial N} x^T$$

$$\frac{\partial \text{loss}}{\partial x} = W^T \frac{\partial \text{loss}}{\partial N}$$

$$\frac{\partial \text{loss}}{\partial b} = \frac{\partial \text{loss}}{\partial N}$$

$$\frac{\partial (\text{cross entropy loss})}{\partial y_j} = \sum_i \begin{cases} t_i (y_i - 1) & i = j \\ t_i y_j & i \neq j \end{cases}$$

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Quiz 9

Consider a convolutional neural network.

Note: **Do NOT consider Biases.**

Input layer:

Input to this CNN are color images of size **264x264x3** with the batch size = **50**

Next layer is Conv2D layer:

number of filters: **12**, filter size: **5x5** ; stride: **3x3** ; padding: **7x7**

What is the shape of the weight matrix for this layer? _____

What is the shape of the output (tensor) of this layer? _____

Next layer is Conv2D layer:

number of filters: **16**, filter size: **4x4** ; stride: **3x3** ; padding: **1x1**

What is the shape of the weight matrix for this layer? _____

What is the shape of the output (tensor) of this layer? _____

Next layer is Max Pooling layer:

pool size: **3x3** ; stride: **2x2** ; padding: **2x2**

What is the shape of the output (tensor) for this layer? _____

Next layer is Flatten layer:

What is the shape of the output (tensor) for this layer? _____

Next layer is Dense layer:

number of nodes: **10**

What is the shape of the weight matrix (tensor) for this layer? _____

What is the shape of the output (tensor) for this layer? _____

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Quiz 9

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Quiz 10

Consider the following performance surface

$$F(X) = 2x_1^2 - 3x_1x_2 + 5x_1 - 4x_2$$

Given the initial point $\begin{bmatrix} 2 \\ 1 \end{bmatrix}$, take **two steps** of the **steepest descent algorithm**, minimizing along a line **at each step**.

You must show the resulting position after each step.

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Quiz 10

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Quiz 11

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Quiz 12

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Quiz 13

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Quiz 14

Consider the expression:

$$f(x, y) = (x * y) - \min\left(\frac{x}{y}, x\right)$$

Given the inputs: $x = 100$, $y = 5$

Draw the computational graph and calculate the $\frac{\delta f(x,y)}{\delta x}$ and $\frac{\delta f(x,y)}{\delta y}$ and show all the numerical values of the forward and backward pass.

For proper credit, you **MUST SHOW** computational graph, numerical values of all local derivatives, all the numerical values as they flow in the forward path, and numerical values in the backward path.

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Quiz 14